



Limiting factors of SAR interferometry

Rüdiger Gens



Causes of decorrelation

$$\gamma = \gamma_{baseline} \gamma_{SNR} \gamma_{Doppler} \gamma_{volume} \gamma_{temporal} \gamma_{atmosphere}$$

$$\gamma = (1 - \delta)$$

$$\gamma = \textit{coherence}$$

$$\delta = \textit{decorrelation}$$

Limiting factors of InSAR

- baseline decorrelation
- thermal noise
- non-overlapping Doppler spectral energy



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Limiting factors of InSAR

- volume scattering
- temporal changes
- atmospheric phenomenon



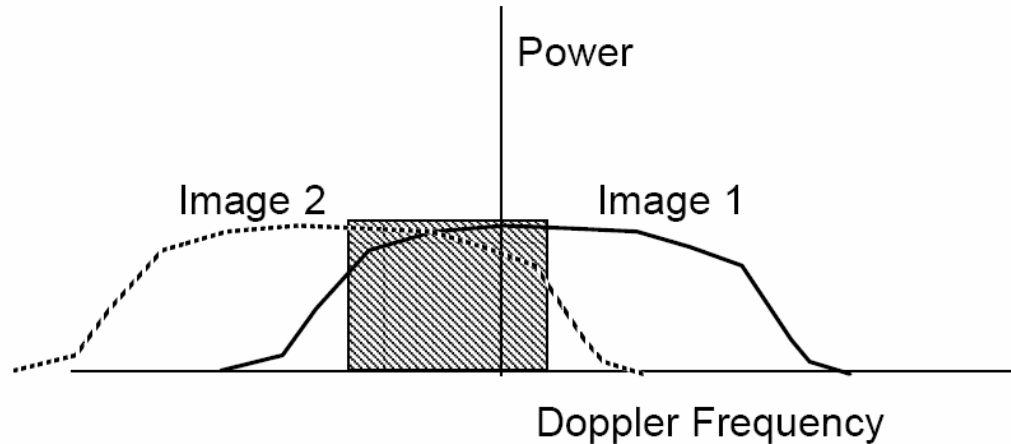
Geometrical decorrelation

- occurs as the separation between the two orbital trajectories (baseline) increases
- correlation coefficient is inversely proportional to the perpendicular baseline component

Limiting factors of InSAR



Non-overlapping Doppler Spectral Energy



Source:
Carande

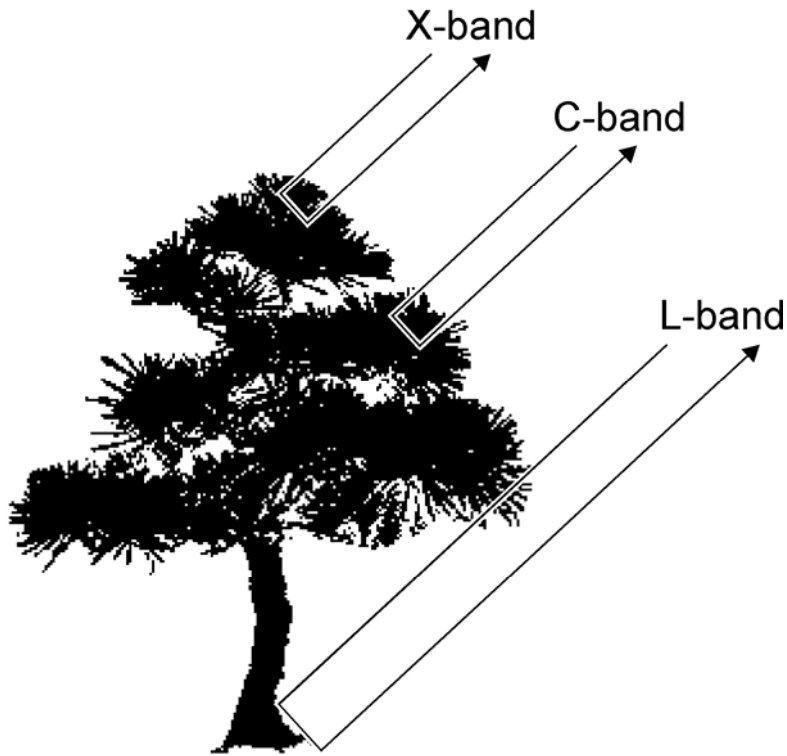
Limiting factors of InSAR

- Doppler spectral width determined by azimuth beam width of SAR
- Doppler center frequency determined by attitude, antenna and earth rotation
- for max coherence, filter out non-overlapping energy



Volume scattering

Limiting factors of InSAR



- scattering from different (random) heights within each resolution cell, such as in volume scattering, produces decorrelation



Temporal decorrelation

- change of scattering within a resolution cell or their electrical properties
 - function of time between the first and the second data acquisition
 - caused by vegetation, wind effects, soil moisture, snow fall, farming activities etc.

Limiting factors of InSAR



Atmospheric perturbation

Limiting factors of InSAR

- ionospheric path delay
 - variations in the total electron content along the path (depends on the time of day and influences the whole scene homogeneously)
 - traveling ionospheric disturbances (cause localized artifacts)
- *tropospheric path delay*
 - dominant dry part
 - small but highly variable wet part which is caused by the strong temporal and spatial variability of the water vapor concentration



Tropospheric water vapor

- probably most limiting factor for differential SAR interferometry
- very localized, heterogeneous effect
 - can cause misinterpretation of deformation fields derived by InSAR in the order of centimeters

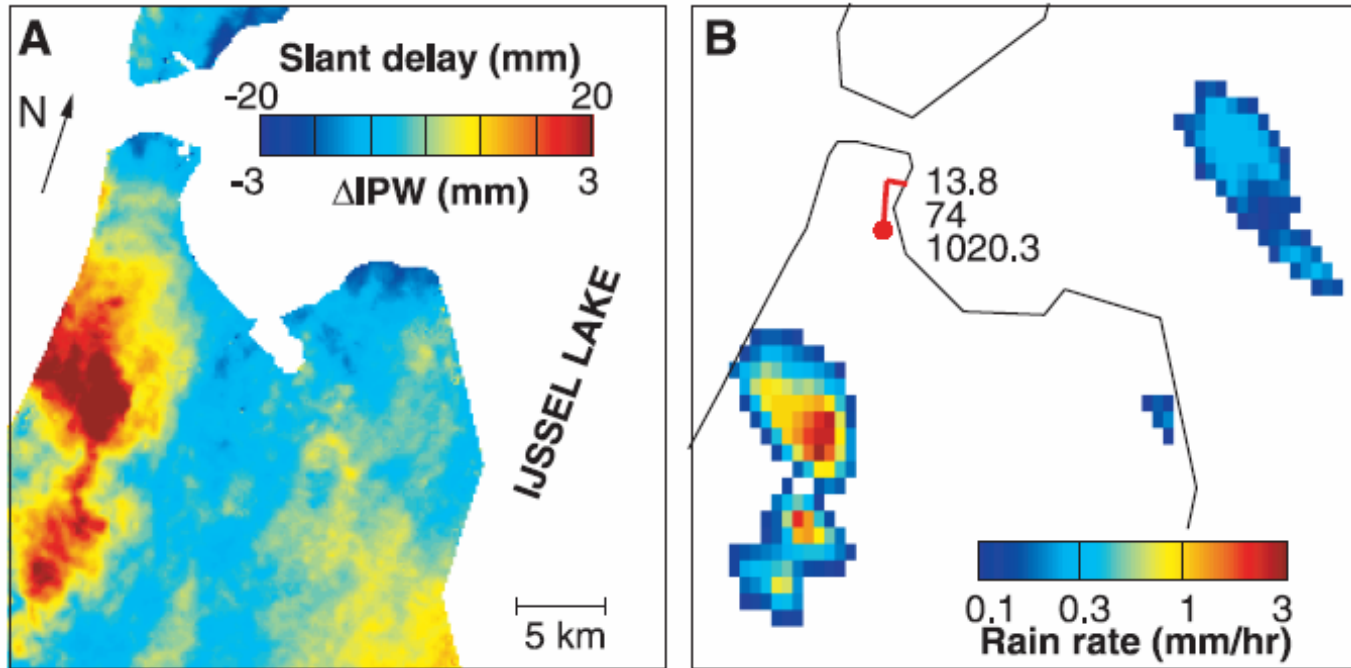
Limiting factors of InSAR



Example: the Netherlands

Effect of precipitation

Limiting factors of InSAR



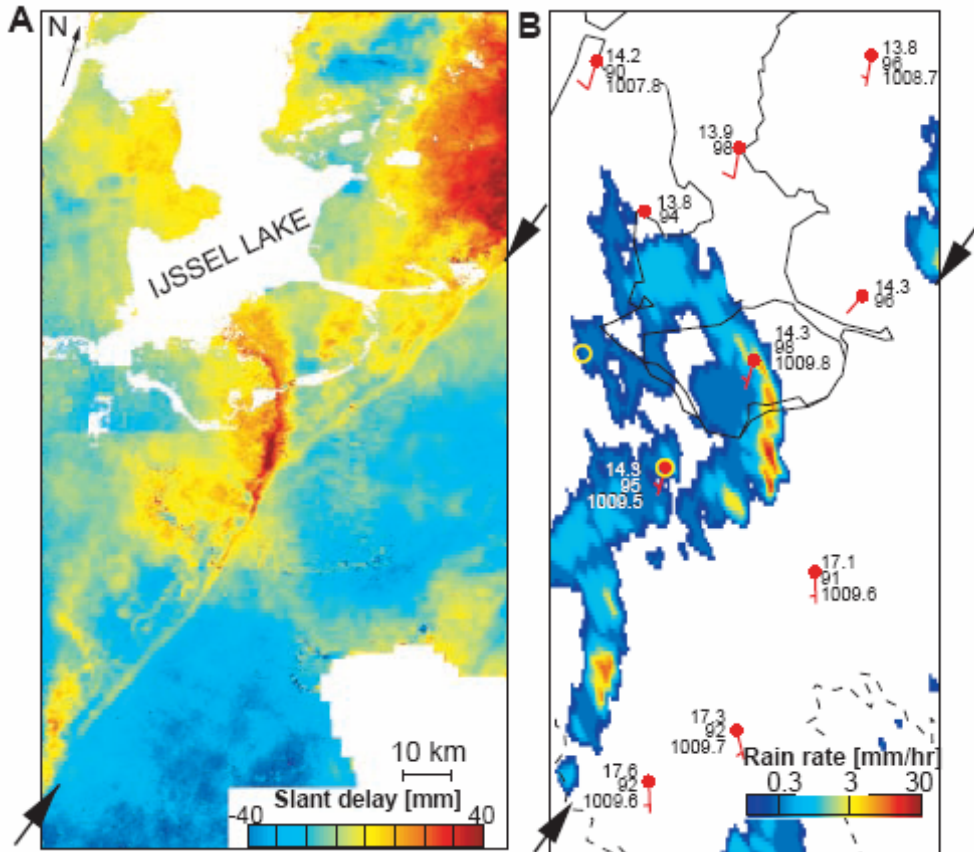
- A: slant delay variation, mapped to zenith-integrated precipitable water differences
- B: weather radar rain rate; surface wind velocity was 4.1 m/s



Example: the Netherlands

Effect of a cold front

Limiting factors of InSAR



- A: cold front is visible as the line between the arrows
- B: weather radar image
 - two weather radar stations are indicated by the yellow circles
 - superposed are surface observations



Orbit errors

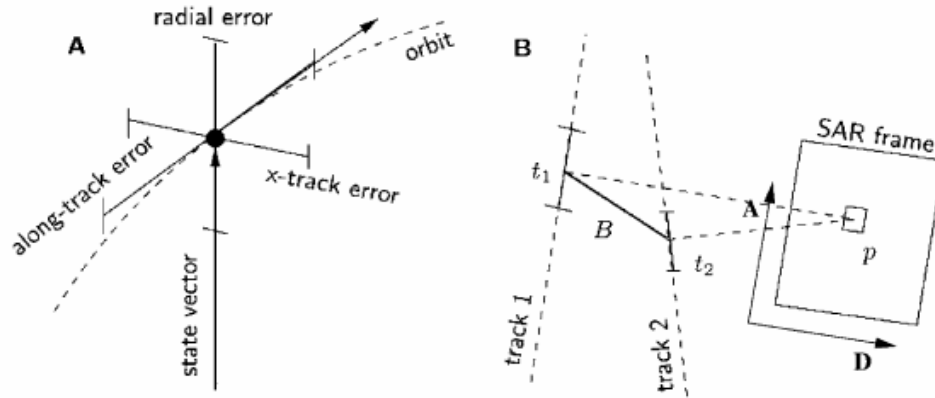


Fig. 3. **A** Three-dimensional sketch of the along-track, across-track and radial error bars. **B** Top view of two converging tracks. Resolution element p is observed at $(t = t_1)$ from the first track 1, and at $(t = t_2)$ from the repeat track 2. The along-track error is indicated by the error bars along the track, (from Hanssen 2001)

- orbital error vector is usually expressed in the coordinate system rotating with the satellite and consists of three components
 - along-track
 - across-track
 - radial



Orbit errors: Filtering approach

- orbital filtering approach can significantly improve precise orbit estimates of short arcs of ERS trajectories in an absolute sense
- approach restricted to those orbital passes in which SAR data were acquired
- limited to determining the across-track and radial components of the orbital trajectory
 - could use timing errors to estimate the along-track error

Limiting factors of InSAR



Orbit errors: Filtering approach

- solving the weighted least-squares orbit determination problem

$$\mathbf{x}^{lsq} = (\mathbf{A}^T \mathbf{W} \mathbf{A})^{-1} \mathbf{A}^T \mathbf{W} \mathbf{d}$$

$$\delta \mathbf{r}_i^{lsq} = \mathbf{r}_i^{lsq} - \mathbf{r}_i^{prior}, \quad \delta \mathbf{r}_i^{lsq} \subseteq \mathbf{x}^{lsq}$$

$$\begin{aligned} n_{12} &= (\mathbf{r}_2^{lsq} - \mathbf{r}_1^{lsq}) - (\mathbf{r}_2^{prior} - \mathbf{r}_1^{prior}) \\ &= \mathbf{B}^{lsq} - \mathbf{B}^{prior} \approx \Delta(\delta \mathbf{r}_{12}) \end{aligned}$$

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